

**Halli Hemingway**

**Defining and Estimating Forest Productivity  
Using Multi-Point Measures and a  
Nonparametric Approach**

University of Idaho, MS Natural Resources  
Advisor: Mark Kimsey, PhD



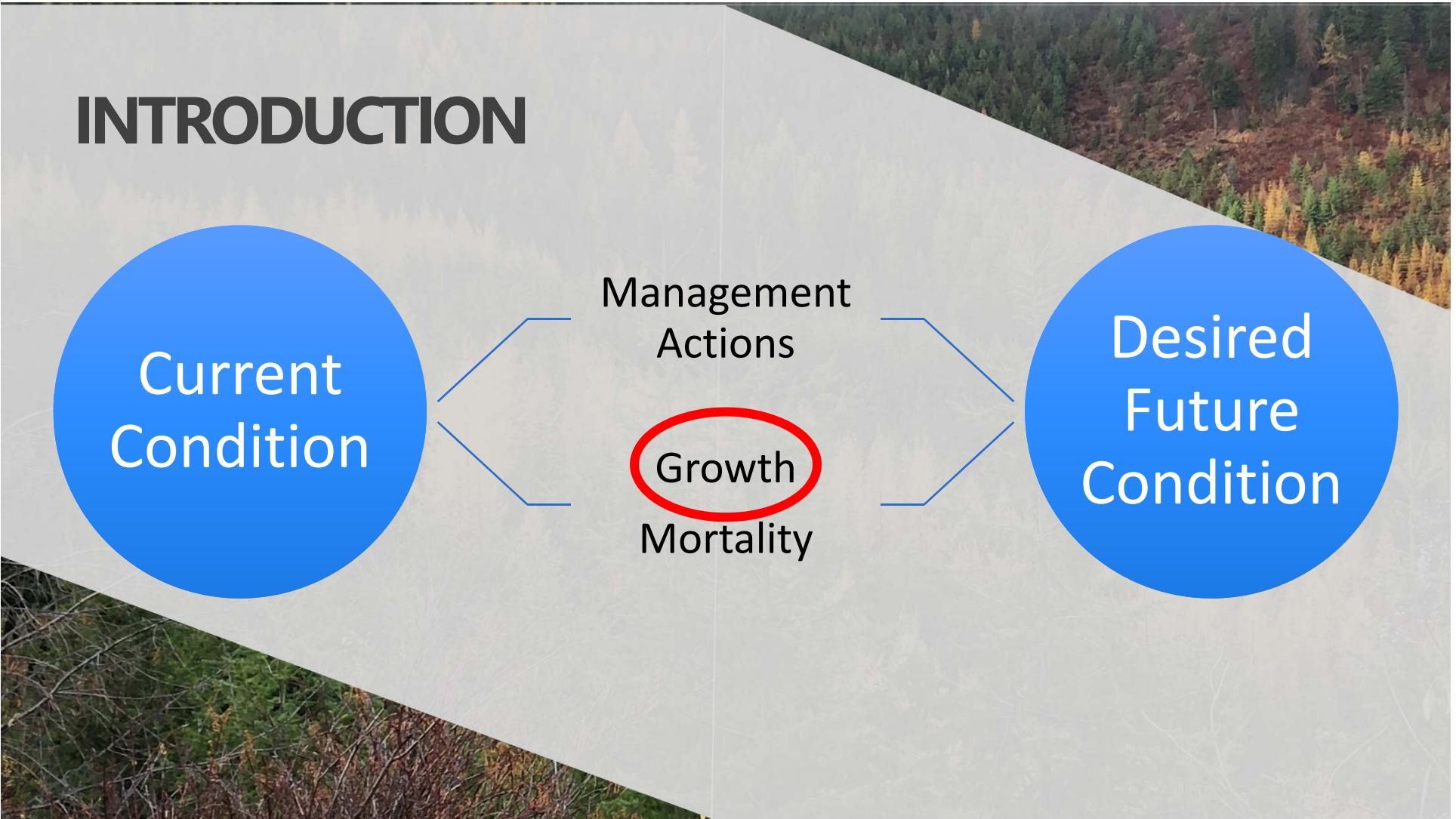
# INTRODUCTION

Current  
Condition

Management  
Actions

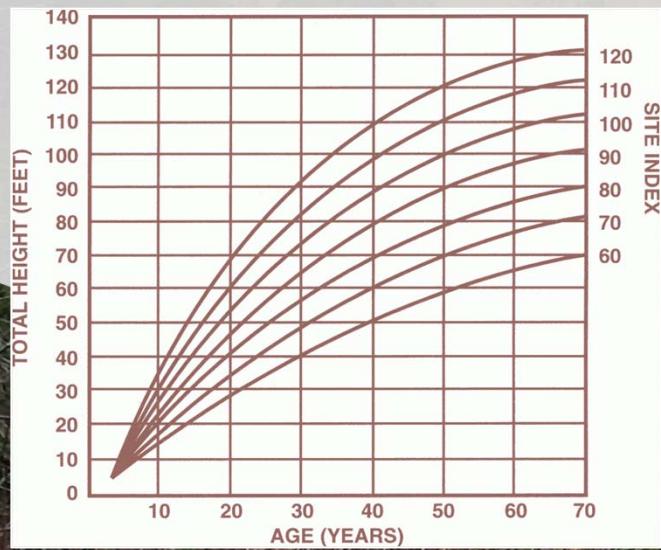
Growth  
Mortality

Desired  
Future  
Condition



# INTRODUCTION

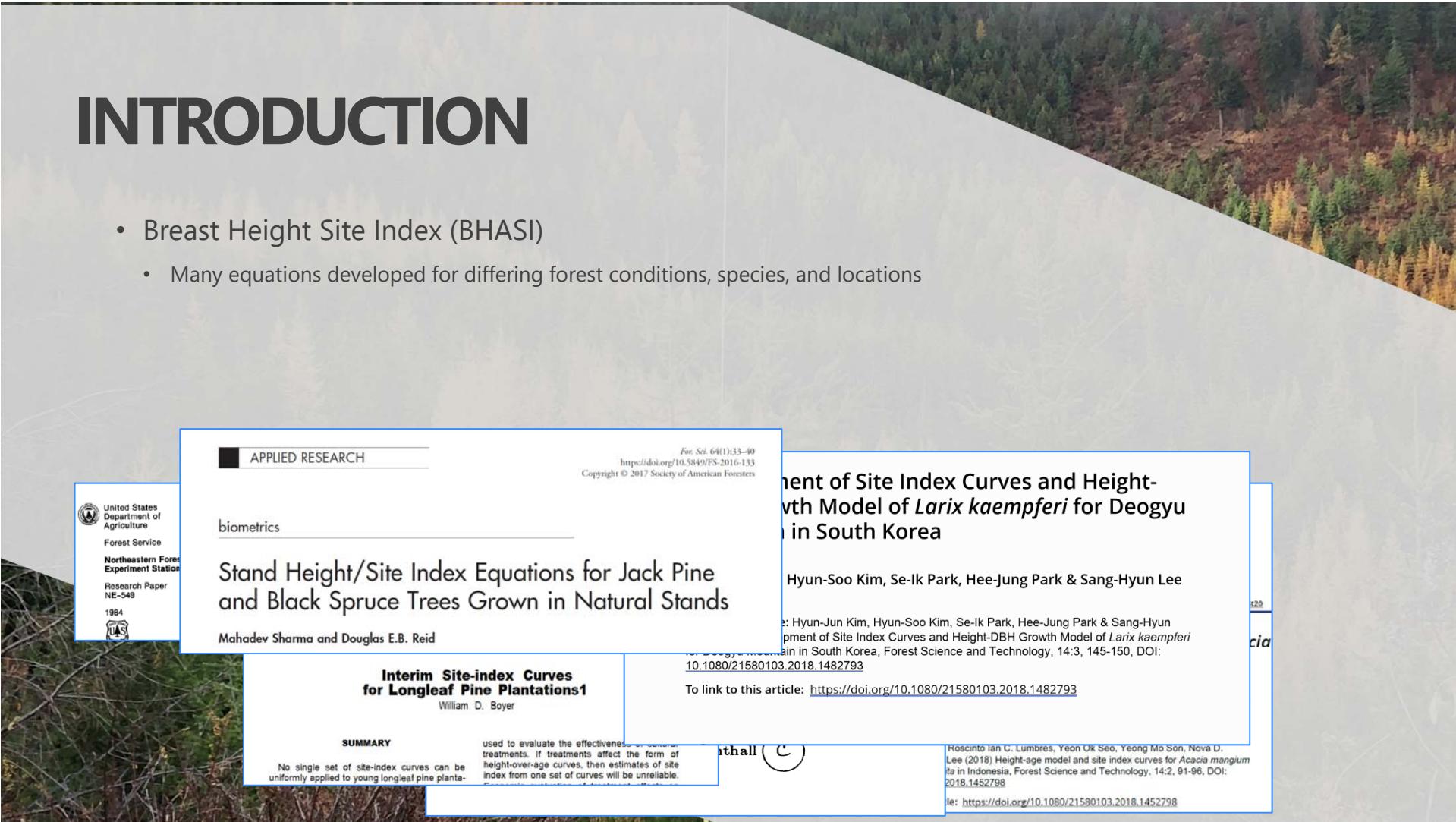
Understanding productivity of forestland is essential in sustainable management and preservation of forest ecosystems (Skovsgaard and Vanclay, 2013; Weiskittel et al., 2011).



The most common measure of forest site productivity is breast height age site index (BHASI) – the expected height at a reference breast height (1.4 m) age. BHASI has been used for over a century to quantify forest productivity (Batho and Garcia, 2006).

# INTRODUCTION

- Breast Height Site Index (BHSI)
  - Many equations developed for differing forest conditions, species, and locations



APPLIED RESEARCH

For. Sci. 64(1):33–40  
<https://doi.org/10.5849/FS-2016-133>  
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biometrics

United States Department of Agriculture Forest Service Northeastern Forest Experiment Station Research Paper NE-549 1984

Stand Height/Site Index Equations for Jack Pine and Black Spruce Trees Grown in Natural Stands

Mahadev Sharma and Douglas E.B. Reid

Interim Site-index Curves for Longleaf Pine Plantations<sup>1</sup>

William D. Boyer

SUMMARY

No single set of site-index curves can be uniformly applied to young longleaf pine plantations. Site index is used to evaluate the effectiveness of treatments. If treatments affect the form of height-over-age curves, then estimates of site index from one set of curves will be unreliable.

To link to this article: <https://doi.org/10.1080/21580103.2018.1482793>

10.1080/21580103.2018.1482793

Roscinto Ian C. Lumbres, Yeon Ok Seo, Yeong Mo Son, Nova D. Lee (2018) Height-age model and site index curves for *Acacia mangium* in Indonesia, Forest Science and Technology, 14:2, 91-96, DOI: 10.1080/21580103.2018.1452798

link: <https://doi.org/10.1080/21580103.2018.1452798>

# INTRODUCTION

The first stem-analysis based site index equations and growth curves for Rocky Mountain Douglas-fir (*Pseudotsuga menziesii* var. *glauca*) in the Inland Northwest, USA were developed by Monserud (1984).

- ❖ Applicable for even-aged, uneven-aged, and mix-species stands
- ❖ No geospatial stratification
  - ❖ Sample equally in 5 habitat types

*Forest Sci.*, Vol. 30, No. 4, 1984, pp. 943-965  
Copyright 1984, by the Society of American Foresters

***Height Growth and Site Index Curves for  
Inland Douglas-fir Based on Stem  
Analysis Data and Forest  
Habitat Type***

ROBERT A. MONSERUD

# INTRODUCTION

## BHASI SHORTCOMINGS



- One height/age measurement
- Disturbance, uneven-aged stands, afforestation, and conversions
- Measurement error
- No systematic landscape scale stratification



# INTRODUCTION: BHASI SHORTCOMINGS

FUNDAMENTAL RESEARCH

*For. Sci.* XXXXX(1-9)  
doi: 10.1093/forec/fzax090  
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## A Multipoint Felled-Tree Validation of Height-Age Modeled Growth Rates

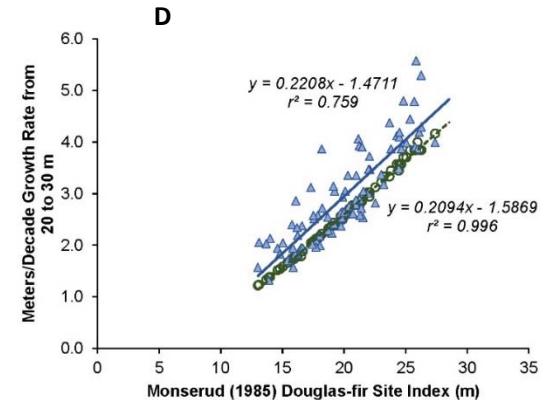
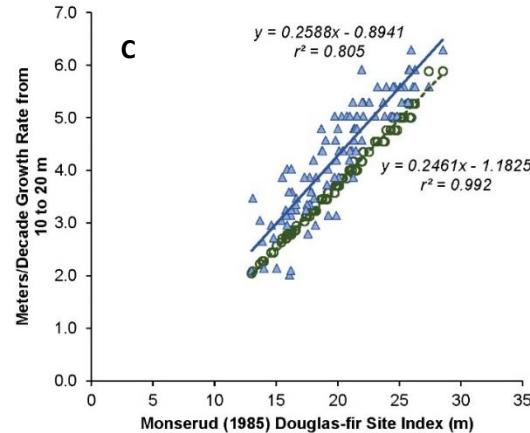
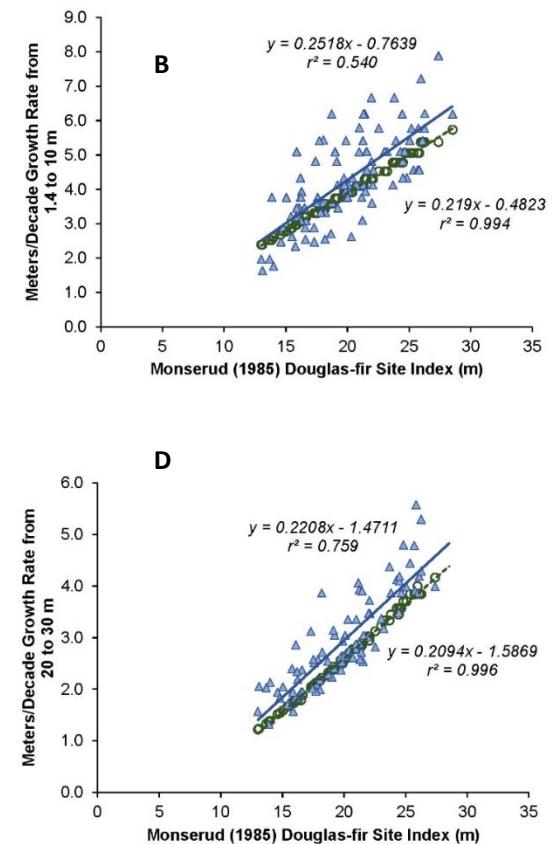
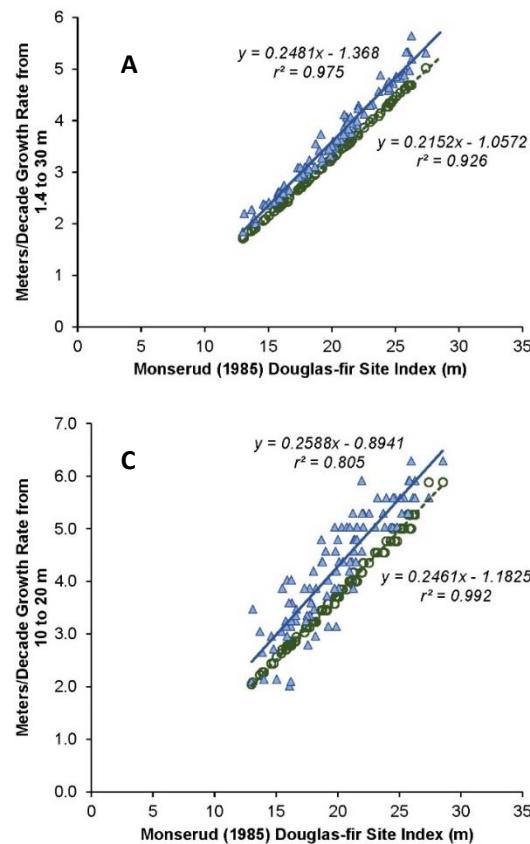
Halli Hemingway<sup>\*</sup> and Mark Kimsey

Accurate measures of forest site productivity are essential for forest-management planning. The most common measure of site productivity is breast height-age site index (BHASI) – the expected height at a reference age. Error from including early growth in productivity estimates and limited applicability of any one BHASI model warrant development of alternative methods. Exploring alternatives may only be necessary if regional BHASI models are not accurately predicting growth rates. We compared modeled height growth rates for Rocky Mountain Douglas-fir (*Pseudotsuga menziesii* var. *glauca*) to felled-tree measurements to evaluate relative performance of a regional BHASI model. An orthogonal sampling design ensured samples were collected across a range of site factors known to influence Douglas-fir growth rates. Growth rates for each 10 m section were calculated and compared to BHASI modeled growth rates. The regional BHASI model underpredicted growth rates from breast height to 30 m. Observed growth rates from 10 to 30 m accounted for the majority of underpredictions relative to BHASI modeled growth rates. An alternative multipoint method of defining site productivity is described. More research comparing BHASI and alternative methods is needed, given the growth rate error associated with one-point site productivity assessment.

Keywords: Douglas fir, site index, forest productivity, height growth



<https://blpi.com/index.php/research/>





# INTRODUCTION: BHASI SHORTCOMINGS

FUNDAMENTAL RESEARCH

For. Sci. XXXX(1-9)  
doi: 10.1093/for/scz090  
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## A Multipoint Felled-Tree Validation of Height-Age Modeled Growth Rates

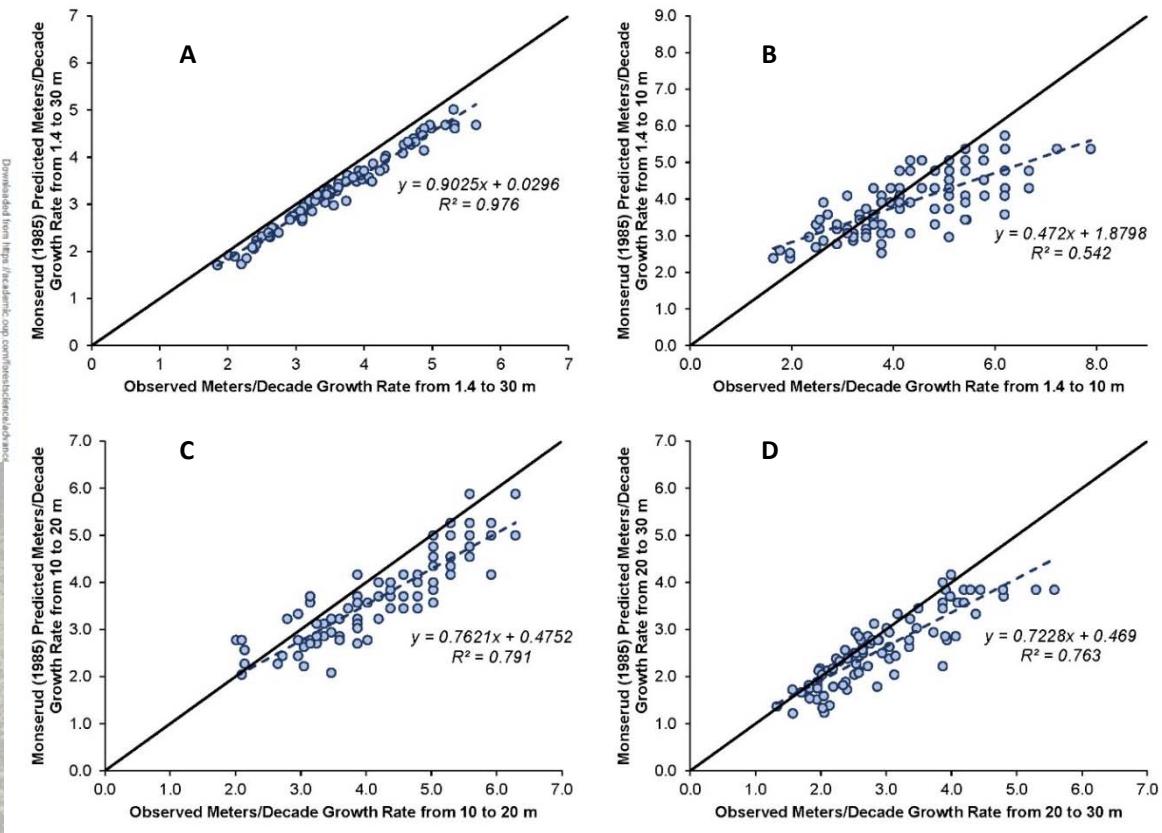
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Keywords: Douglas-fir, site index, forest productivity, height growth



<https://blpi.com/index.php/research/>



# INTRODUCTION

Estimating forest productivity across large landscapes indirectly using environmental variables.

- ❖ Direct productivity measures
- ❖ Geocentric approach
- ❖ Balanced sampling across factors influencing tree growth
- ❖ Attention to problem of correlations of predictors
- ❖ Problems with multiple interacting predictors
- ❖ Nonparametric multiplicative regression
- ❖ Abandon simplistic assumptions and embrace interaction

**Forestry** *An International Journal of Forest Research*



Forestry 2014; **87**, 109–128, doi:10.1093/forestry/cpt034  
Advance Access publication 11 November 2013

## Predictive approaches to forest site productivity: recent trends, challenges and future perspectives

Jean-Daniel Bontemps<sup>1,2\*</sup> and Olivier Bouriaud<sup>3</sup>



<sup>1</sup>AgroParisTech, Centre de Nancy, UMR 1092 INRA/AgroParisTech LERFoB, (Laboratoire d'Etude du Climat et ses Applications), 14 rue Girardet, Nancy 54000, France  
<sup>2</sup>INRA, UMR 1092 INRA/AgroParisTech LERFoB (Laboratoire d'Etude du Climat et ses Applications), 14 rue Girardet, Nancy 54000, France  
<sup>3</sup>Universitatea din Suceava, Faculty of Forestry, Suceava, 9 str. Universitatii, Suceava 71000, Romania

\*Corresponding author. E-mail: jdbontemps.agroparistech@gmail.com

Received 5 February 2013



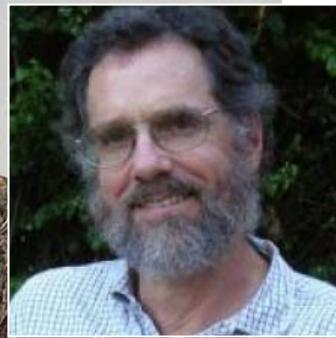
*Journal of Vegetation Science* 17: 819–830, 2006  
© IAVS; Opulus Press Uppsala.

819

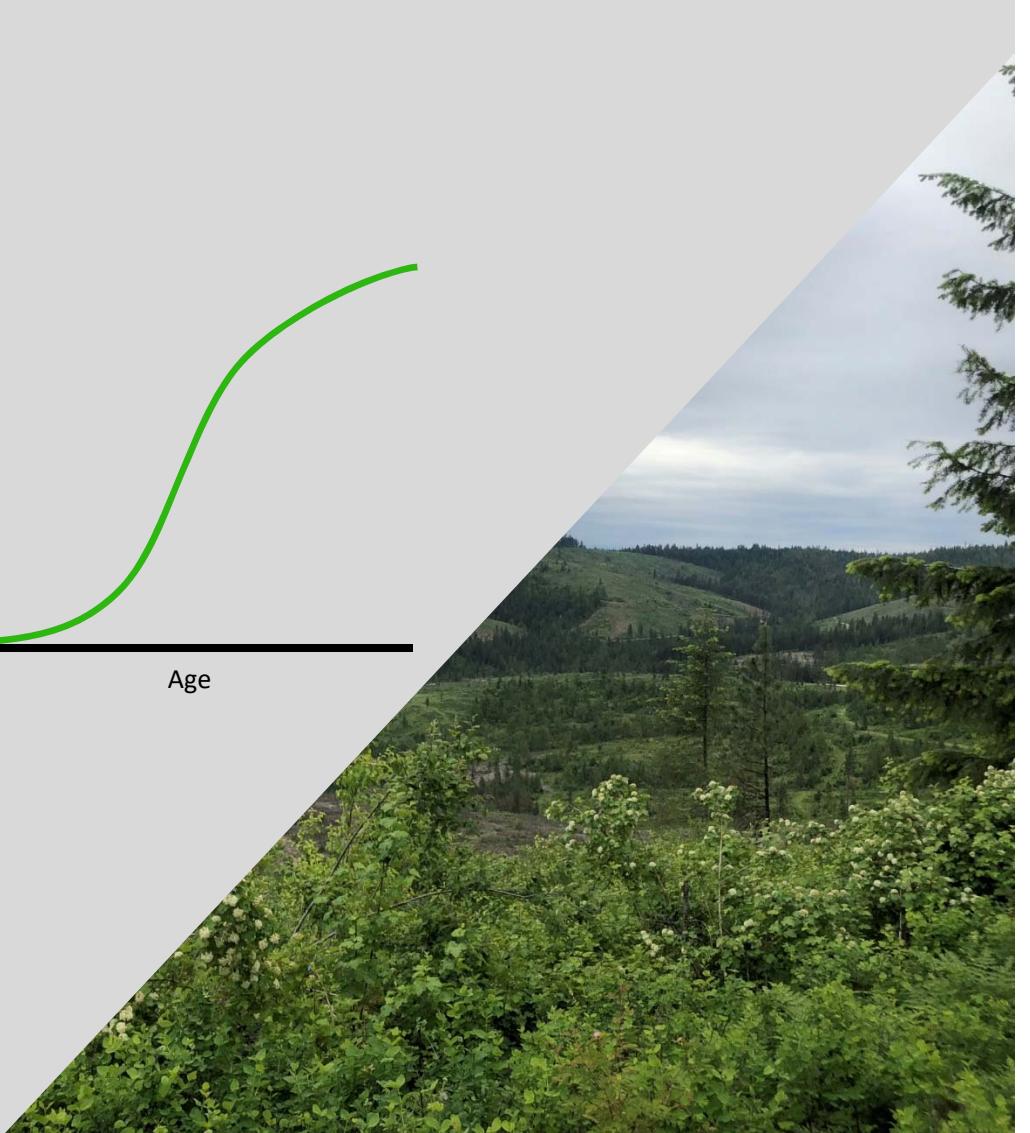
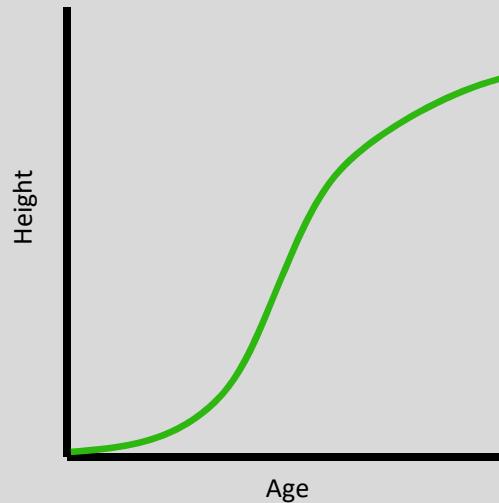
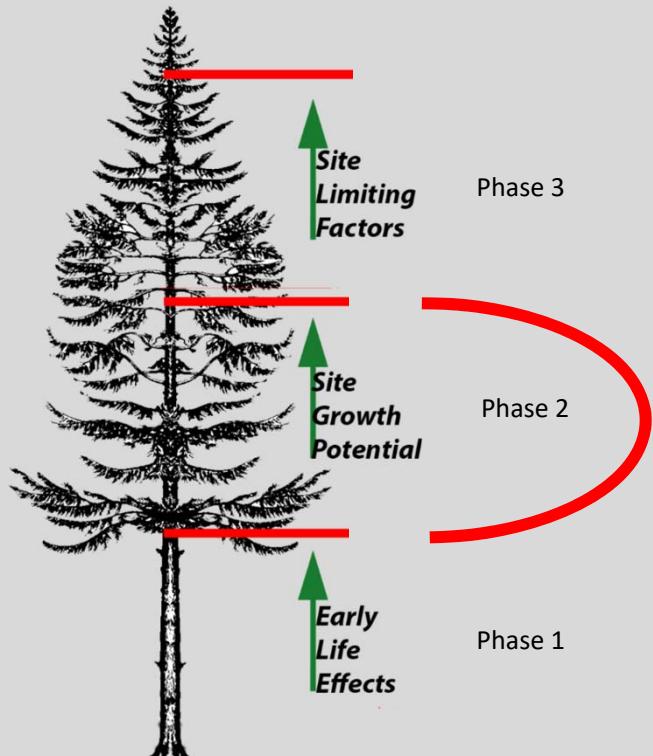
## Non-parametric habitat models with automatic interactions

**McCune, Bruce**

Department of Botany and Plant Pathology, Oregon State University, Corvallis, OR 97331 USA;  
E-mail [Bruce.McCune@science.oregonstate.edu](mailto:Bruce.McCune@science.oregonstate.edu)



# INTRODUCTION



**10-Meter Site Index** (Arney, 2017)

# INTRODUCTION



The Forest Projection and Planning Software (FPS)  
->Forest Biometrics Research Institute



FPS used by 82 forestry organizations managing over 4.8 million hectares



Accuracy of FPS 10-meter site index predictions?



FPS modeling strategies and parameters?



# RESEARCH OBJECTIVES



Determine if the Monserud regional BHASI model is accurately predicting tree height growth rates

Yes



Explore nonparametric approaches of modeling BHASI

No



Determine relative accuracy of FPS predicted 10-Meter Site Index



Produce and evaluate GIS maps of BHASI for the study area



Explore alternative, non-parametric modeling parameters and approaches



Produce and evaluate GIS maps of 10-Meter Site Index for the study area

# METHODS: STUDY AREA



1.3 million acres

## Range

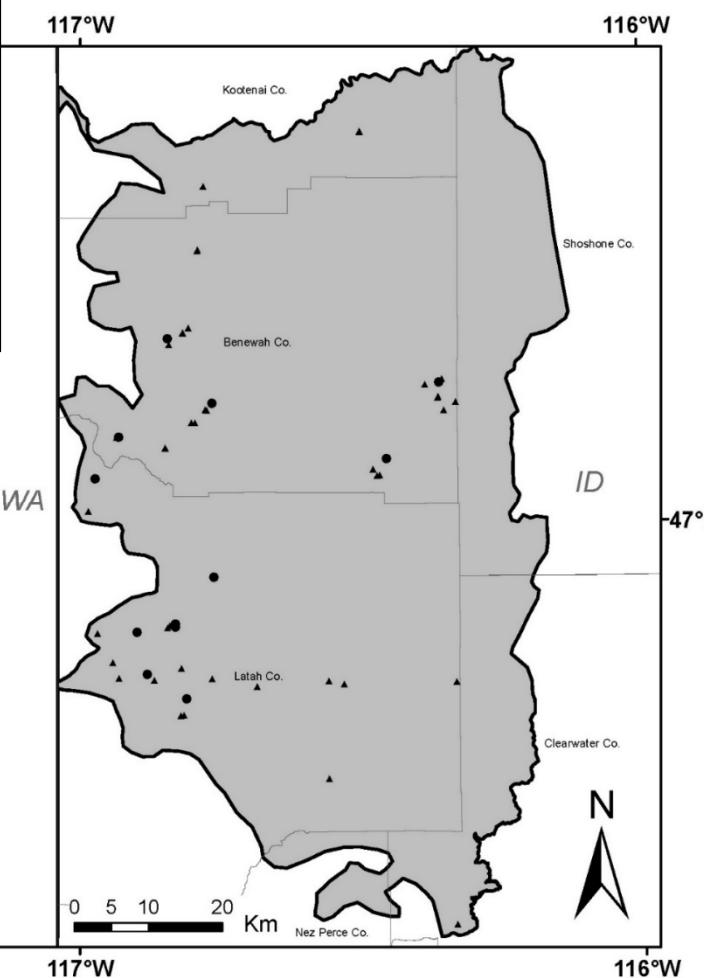
Elevation 965 – 6,358 ft

Mean Annual Precipitation 19 – 63 in

Soil Depth 13 - >80 in



Douglas-fir chosen as the test species



# METHODS: STUDY AREA STRATIFICATION



One-acre point grid applied to study area



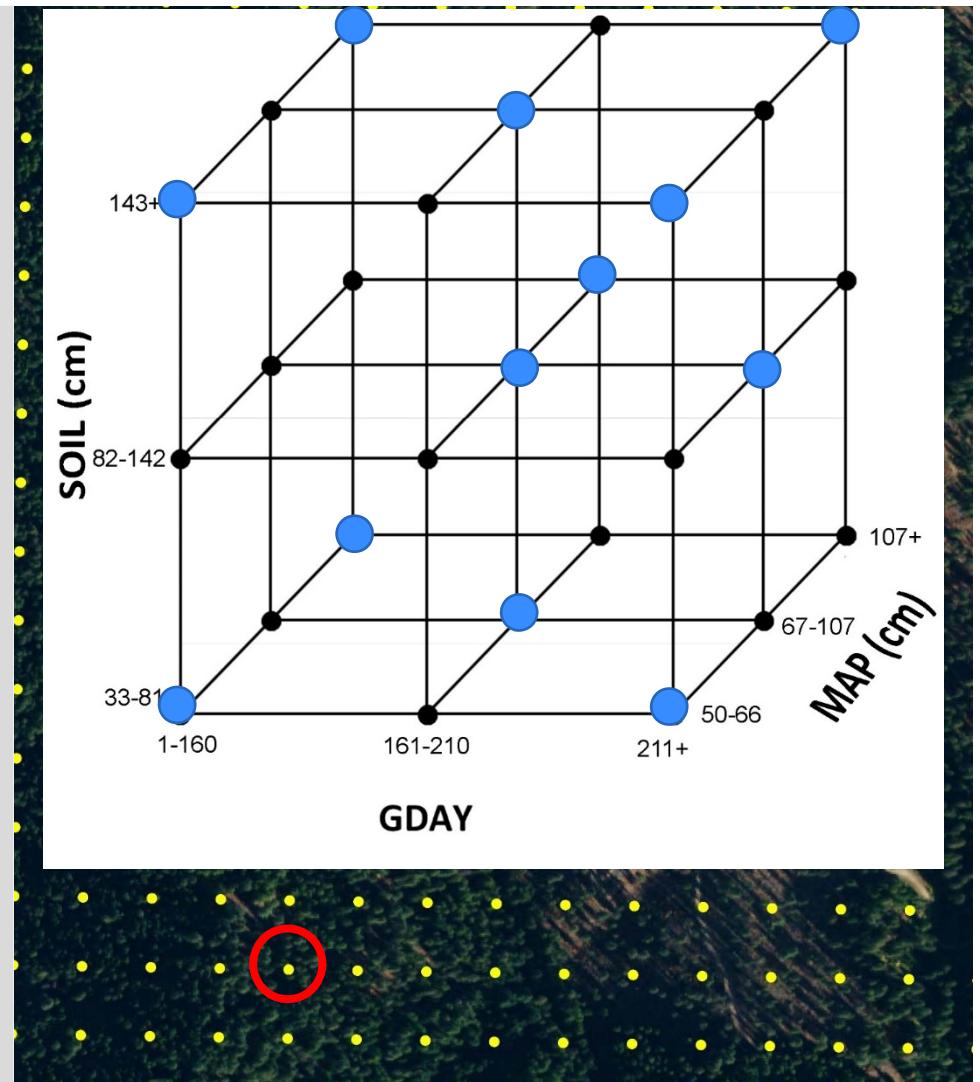
Balanced orthogonal sample



Sample sites randomly selected from  
27 strata



44 sample sites  
12 validation sites



# METHODS: SAMPLING



2-5 dominant or codominant Douglas-fir selected and felled



Sectioned at stump, breast height, 10, 20, and 30 meters



Ring counts at each section



Total tree height measured



Soil depth verified



# METHODS: SAMPLING

10-20 m growth rate calculated on site

$$10MSI = \frac{10YRS \times 10m}{RC_{10} - RC_{20}}$$

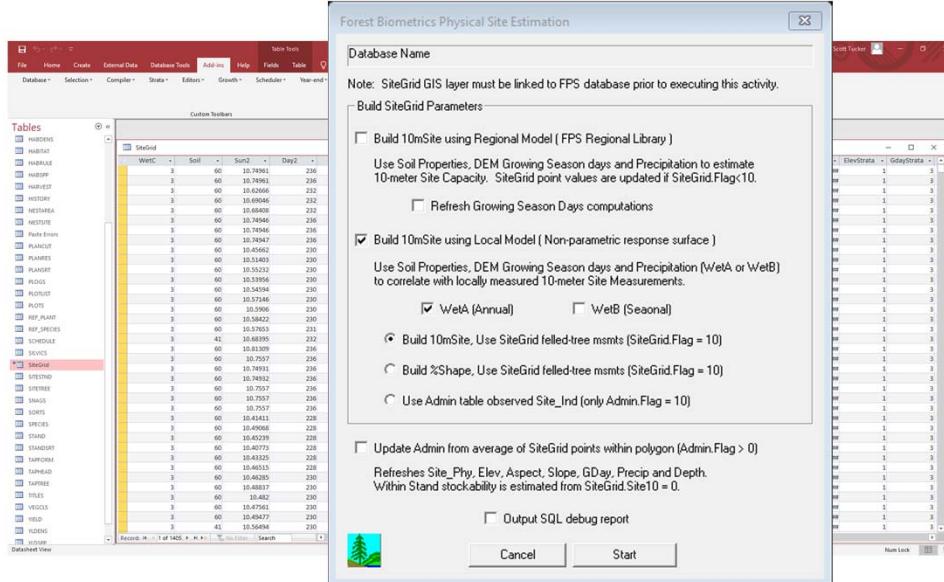
Sample trees growth rates within 1 m/d

Tree Silviculture, Site, and Taper Record							
Tree #	1	Species		Location	Crystal Creek		
Date:	/	/	/	Site Tree?	Yes	No	
#	dob	dbt	dst	Leng	Yrs	Sap	Comments
9.	top			18.5			Tree Top
8	65.05	33	23				Near 100-ft ht
7	137.075	33	46				Near 67-ft ht
6	176.10	33	65				Near 34-ft ht
5							Crown Base
4							80% of DBH
3							Near 21-ft ht
2	217.25	35	87				Breast ht
1	248.35	1.0	90				Stump ht
Total Height (sum of lengths) _____							
dob = diameter outside bark at this point							
dbt = double bark thickness at this point							
dst = double sapwood thickness at this point							
Leng = length in feet of this log segment							
Yrs = total ring count (age) from pith at this point							
Sap = sapwood-only ring count (years) at this point							
Elevation:	3462	Years 0-10	25				
Slope %:	20	Years 10-20	19				
Soil Depth:	60	Years 20-30	23				
Recorder	Precip: 45	Yrs = total ring count (age) from pith at this point	53	10MSI			
Cruiser		Sap = sapwood-only ring count (years) at this point					

Tree Silviculture, Site, and Taper Record							
Tree #	2	Species		Location			
Date:	/	/	/	Site Tree?	Yes	No	
#	dob	dbt	dst	Leng	Yrs	Sap	Comments
9	top			19.5			Tree Top
8	51.05	33	18				Near 100-ft ht
7	121.05	33	39				Near 67-ft ht
6	147.10	33	58				Near 34-ft ht
5							Crown Base
4							80% of DBH
3							Near 21-ft ht
2	182.20	35	78				Breast ht
1	218.30	1.0	84				Stump ht
Total Height (sum of lengths) _____							
dob = diameter outside bark at this point							
dbt = double bark thickness at this point							
dst = double sapwood thickness at this point							
Leng = length in feet of this log segment							
Yrs = total ring count (age) from pith at this point							
Sap = sapwood-only ring count (years) at this point							
Elevation:	626	Years 0-10	26				
Slope %:	26	Years 10-20	19				
Soil Depth:	60	Years 20-30	23				
Recorder	Precip: 45	Yrs = total ring count (age) from pith at this point	53	10MSI			
Cruiser		Sap = sapwood-only ring count (years) at this point					



# METHODS: GENERATING FPS 10MSI PREDICTIONS



Generate 10-Meter Site Index predictions across our study area using FPS and the process in Arney (2017).

Input 44 sample location 10-Meter Site Index measurements, sample site MAP, SOIL, and GDAY.

Input 1-acre point grid populated with MAP, SOIL, and GDAY.

FPS uses nonparametric regression with a locally weighted smoothing parameter to estimate 10-meter site index for unsampled locations.

SPAN = 1

# METHODS: EVALUATING OPTIMUM SMOOTHING SPAN

The figure shows a screenshot of the RStudio interface. The left panel displays R code for performing an ANCOVA analysis. The right panel shows a residual plot with a normal distribution curve overlaid.

```

library(rgeos)
library(spdep)
library(gstat)
library(foreign)
# ...
# RMSE loss with GDA, META, SILL, and ELEV & span=0.81
# with direct prediction in there is no interpolation
# I # used the uses-as function to get the optimum span for this model
# ...
# ss10M <- readRDS(file.choose(), "44sampleSites_Corrected")
sb <- readRDS(file.choose(), "ForestedStudyArea")
# ...
plot(ss10M)
plot(sb)
# ...
NRC5_30_SITES <- readR("C:/Users/Hall11/Dropbox (BLPI)/H.Hemingway/Projects/Dropbox/GradSchool/Chapter2/NRC5_30_SITES.RData")
# ...
valsites <- readRDS(file.choose(), "validationsites")
# ...
summary(valsites)
# ...
summary(ss10M)
# ...
FTSM_tot <- lm(ss10M$SILL_D_ss10M|weta_D_ss10M|day3,D, ss10M$siteID,
  degree = 2, criterion = "cv", user.span = NULL, plot = TRUE)
# ...
summary(FTSM_tot)
# ...

```

Control settings:  
 span : 1.0401816  
 degree : 2  
 fast : FALSE  
 surface : interpolate  
 normalize: TRUE  
 parametric: FALSE  
 degree : 2  
 Error in if (sum(!is.na(output)) > 80) { :  
 missing value where TRUE/FALSE needed

Environment History Connections

Global Environment

- 0 Dta10 100 obs. of 9 variables
- a1 List of 13
- a2 List of 13
- a3 List of 13
- BH.10pmgrowthrate 10^7 obs. of 3 variables
- BH10 198 obs. of 4 variables

Res Photo Packages Help Viewer

Plot showing residuals (r.squared) versus x. The plot includes a normal distribution curve overlaid on the data points.

LOESS model 10MSI = f(MAP+GDAY+SOIL)

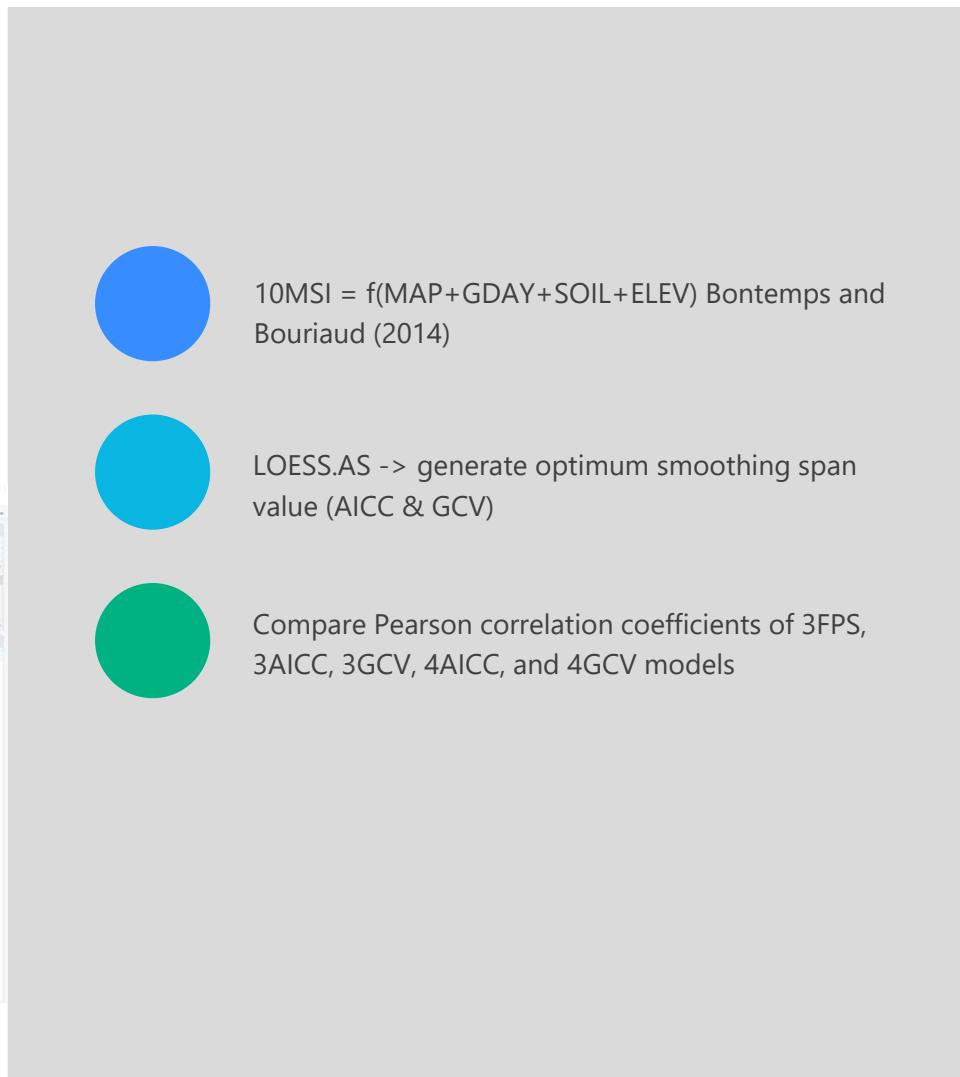
LOESS.AS -> generate optimum smoothing span value (AICC & GCV)

Compare Pearson correlation coefficients of 3FPS, 3AICC, and 3GCV models

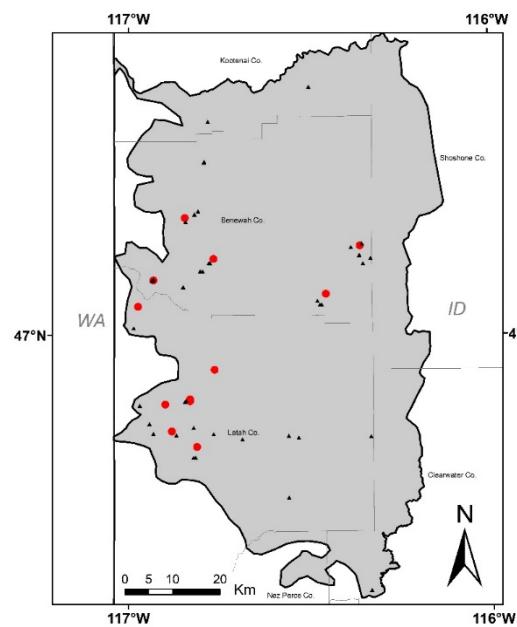
# **METHODS: CREATING AN ALTERNATIVE 10MSI MODEL**

The screenshot shows the RStudio interface with the following details:

- Script Editor:** Displays an R script for ANCOVA analysis. The code includes reading data from CSV files, performing ANCOVA with post-hoc Tukey HSD tests, and plotting the results. A specific section of the code is highlighted in yellow.
- Plot Window:** Shows a scatter plot of  $MPG$  versus  $dis$ . The x-axis is labeled  $dis$  and ranges from approximately 5e+08 to 2e+09. The y-axis is labeled  $MPG$  and ranges from 10 to 40. A blue curve represents a fitted model, showing a non-linear relationship where MPG increases with distance up to a point and then levels off.
- Environment View:** Shows the global environment with objects like `dis3D`, `disdata`, `disresults`, `disresults30`, and `FTSE_104`.
- Console View:** Displays the output of the R code execution, including the number of parameters, degrees of freedom, and trace of the residual matrix.



# METHODS: VALIDATING FPS AND ALTERNATIVE MODEL PREDICTIONS

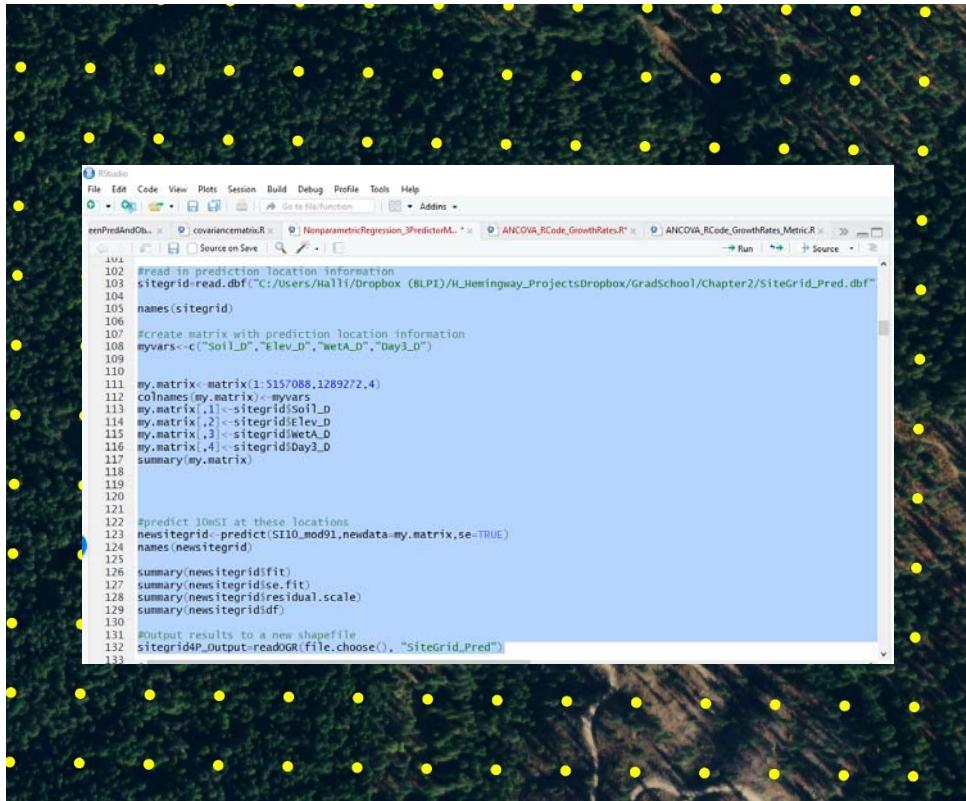


Compare model predicted and observed 10MSI at each of the 12 validation sites. Models: 3FPS, 3AICC, 3GCV, 4AICC, and 4GCV

Calculated 80% confidence interval for each model predicted 10MSI

Determined if the observed 10MSI was within the 80% confidence interval of the models' predicted 10MSI

# METHODS: RASTER MAP PRODUCTION

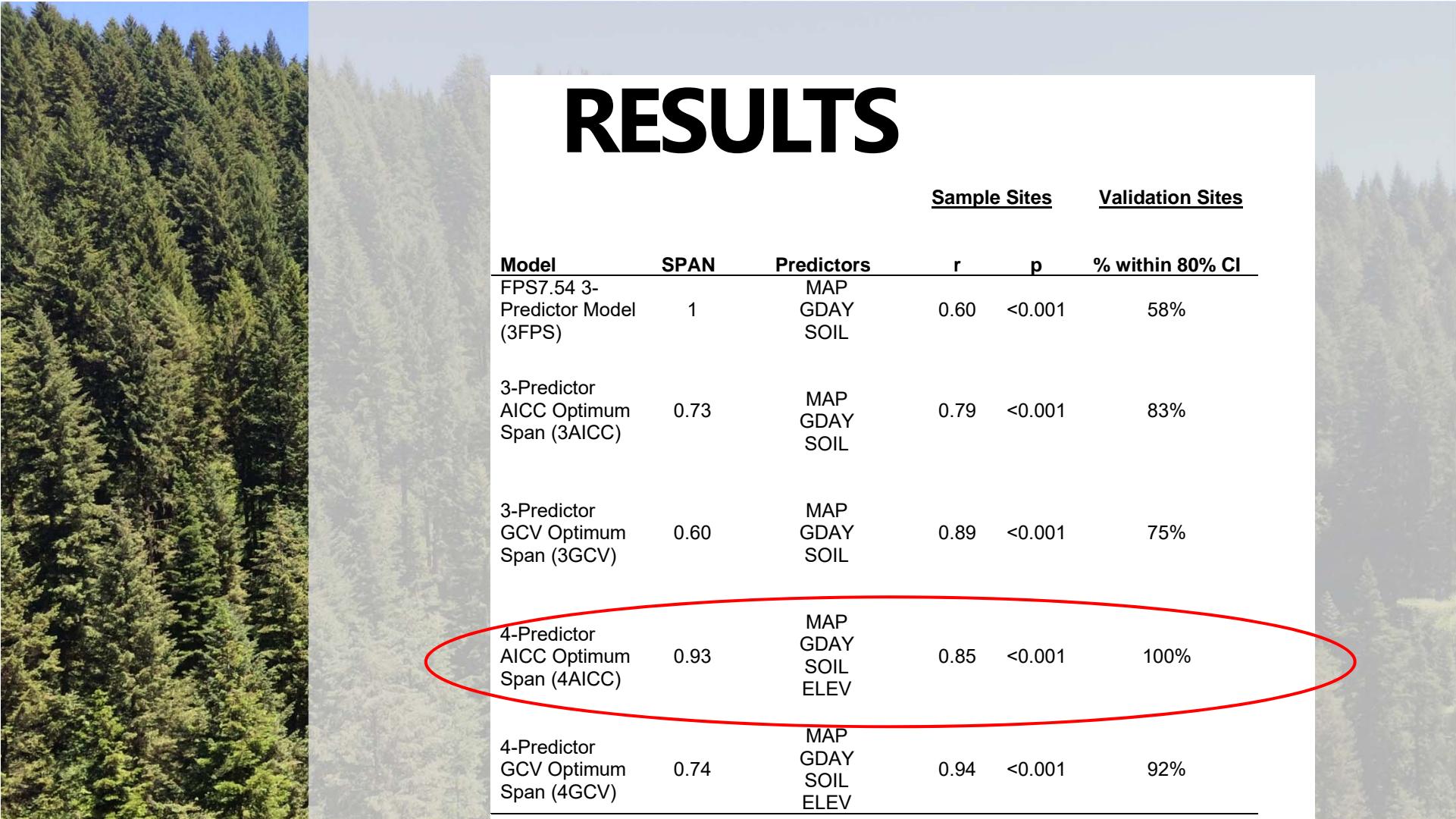


Applied best model to 1-acre point grid of unsampled locations -> predict()

Predicted 10-meter site index and standard error for each grid point

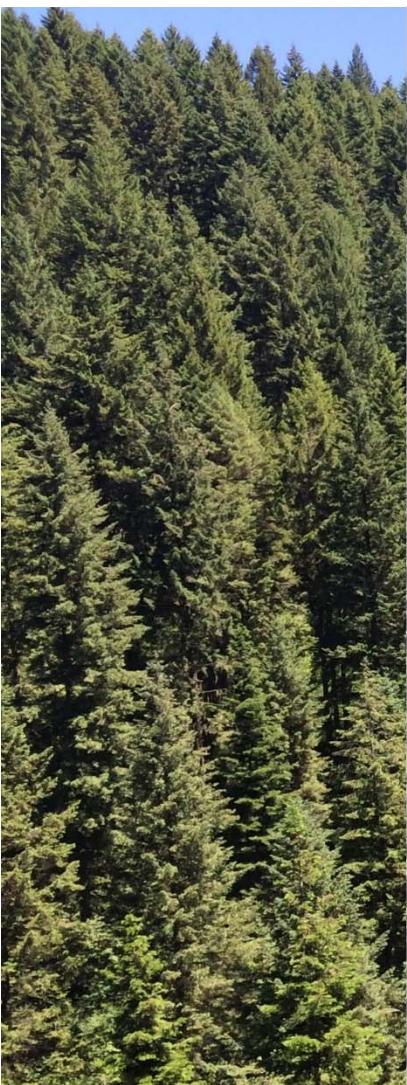
Grid points with predictions outside the range of sampled 10-meter site index removed

Point grids converted to raster datasets with a 1-acre grid size.

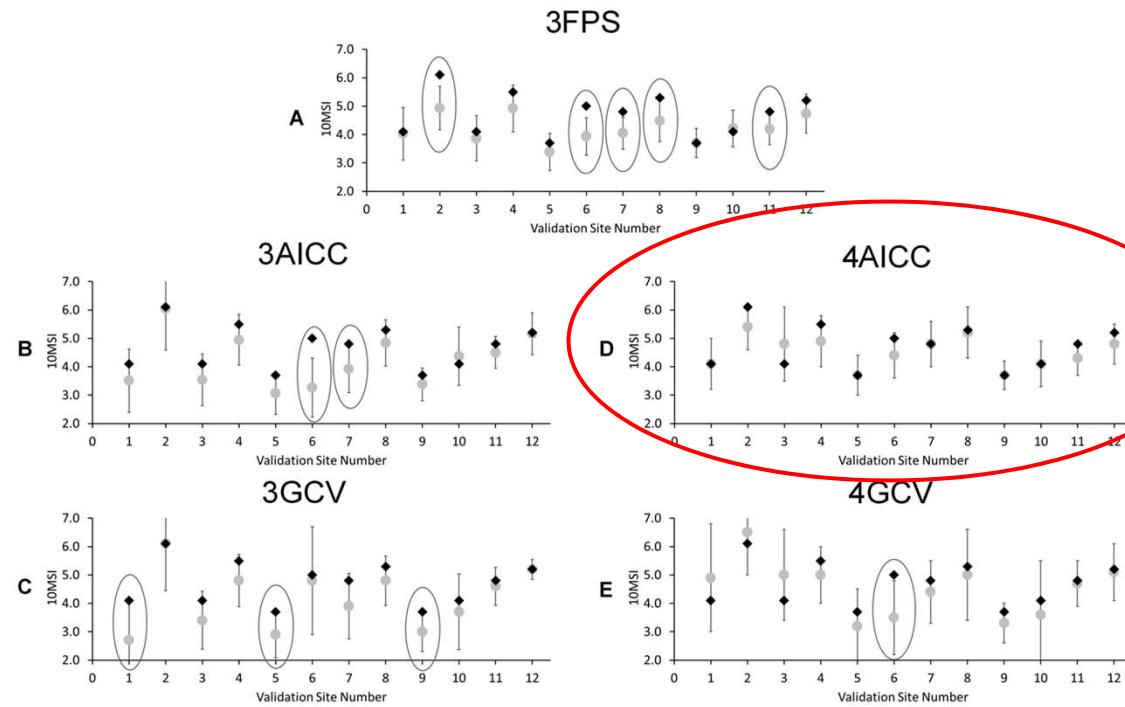


# RESULTS

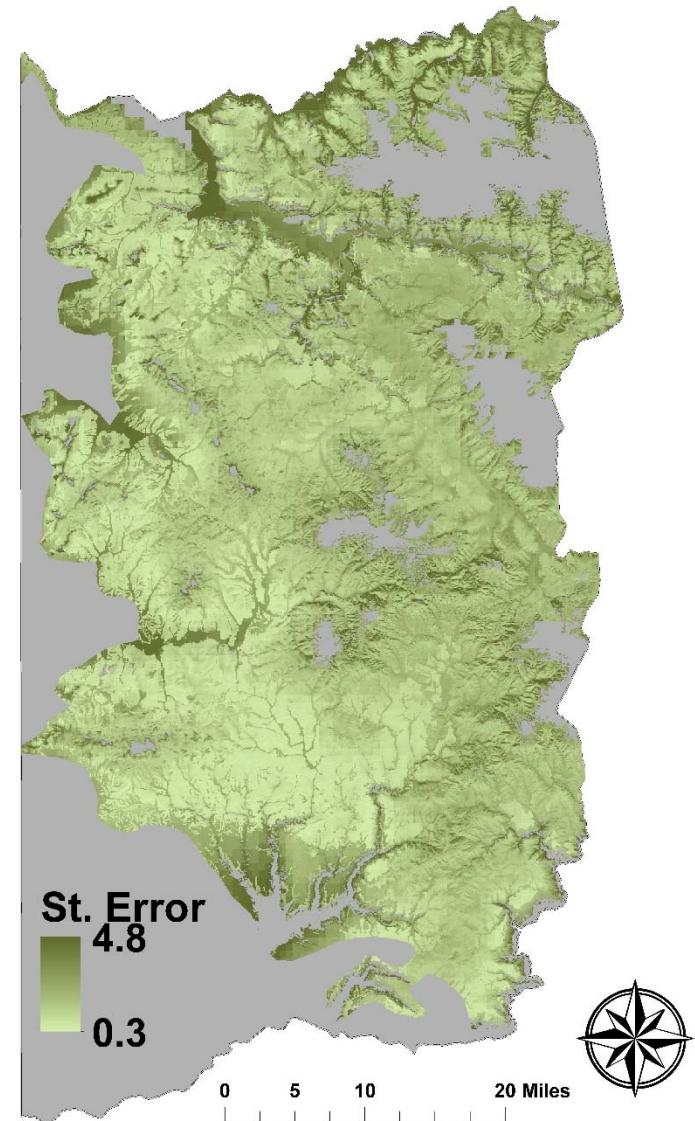
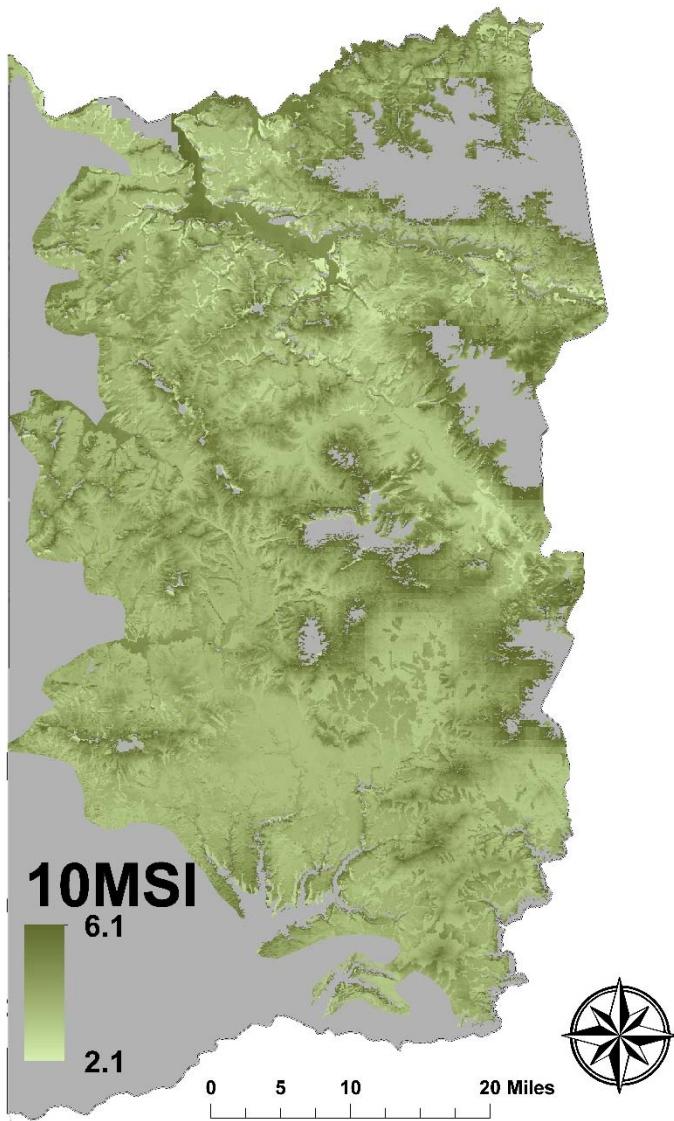
<u>Model</u>	<u>SPAN</u>	<u>Predictors</u>	<u>r</u>	<u>p</u>	<u>% within 80% CI</u>
FPS7.54 3-Predictor Model (3FPS)	1	MAP GDAY SOIL	0.60	<0.001	58%
3-Predictor AICC Optimum Span (3AICC)	0.73	MAP GDAY SOIL	0.79	<0.001	83%
3-Predictor GCV Optimum Span (3GCV)	0.60	MAP GDAY SOIL	0.89	<0.001	75%
4-Predictor AICC Optimum Span (4AICC)	0.93	MAP GDAY SOIL ELEV	0.85	<0.001	100%
4-Predictor GCV Optimum Span (4GCV)	0.74	MAP GDAY SOIL ELEV	0.94	<0.001	92%

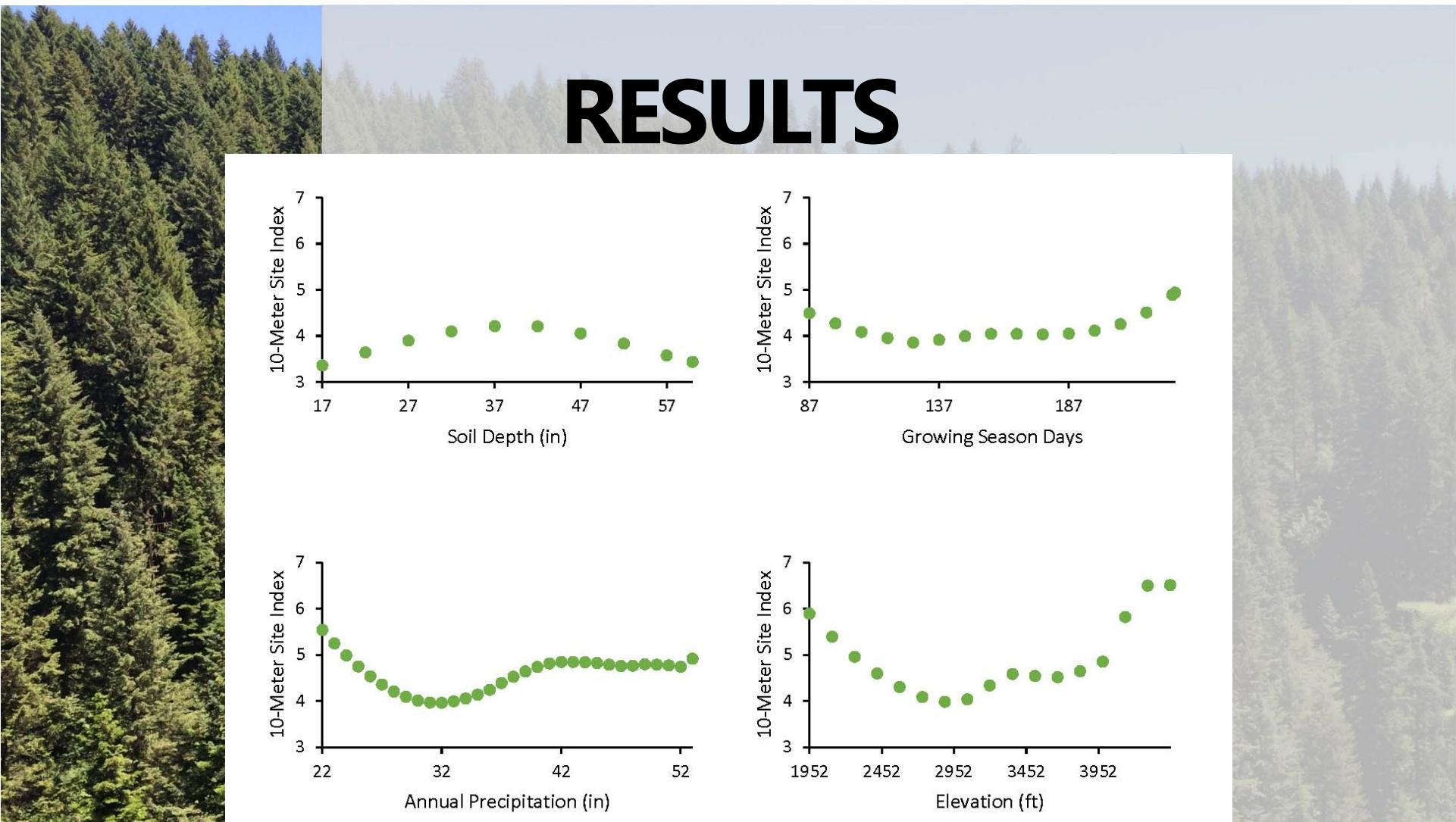


# RESULTS

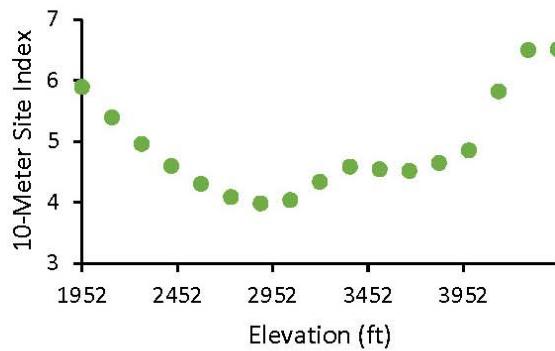
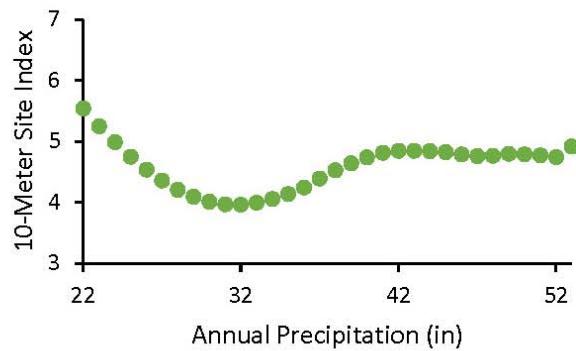
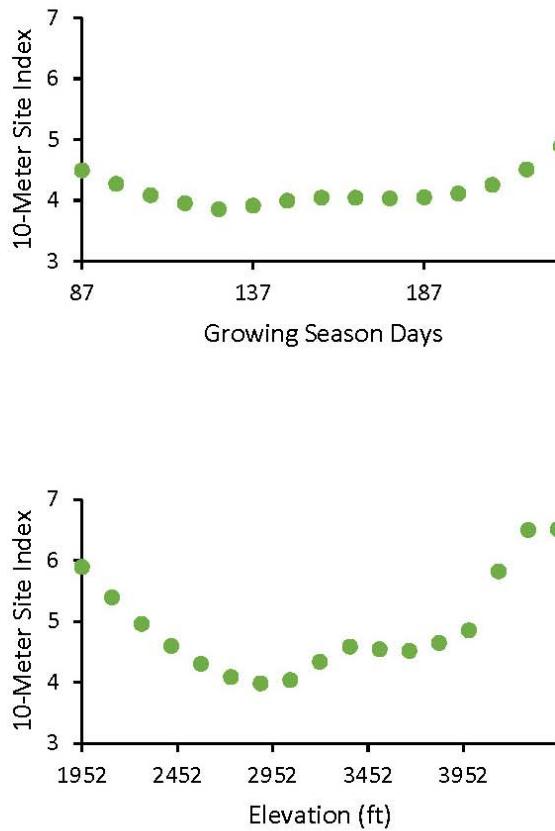
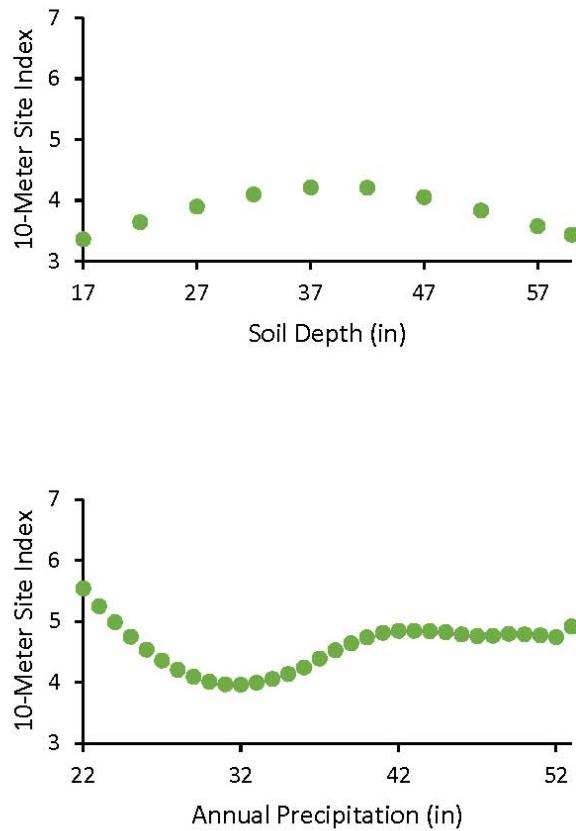


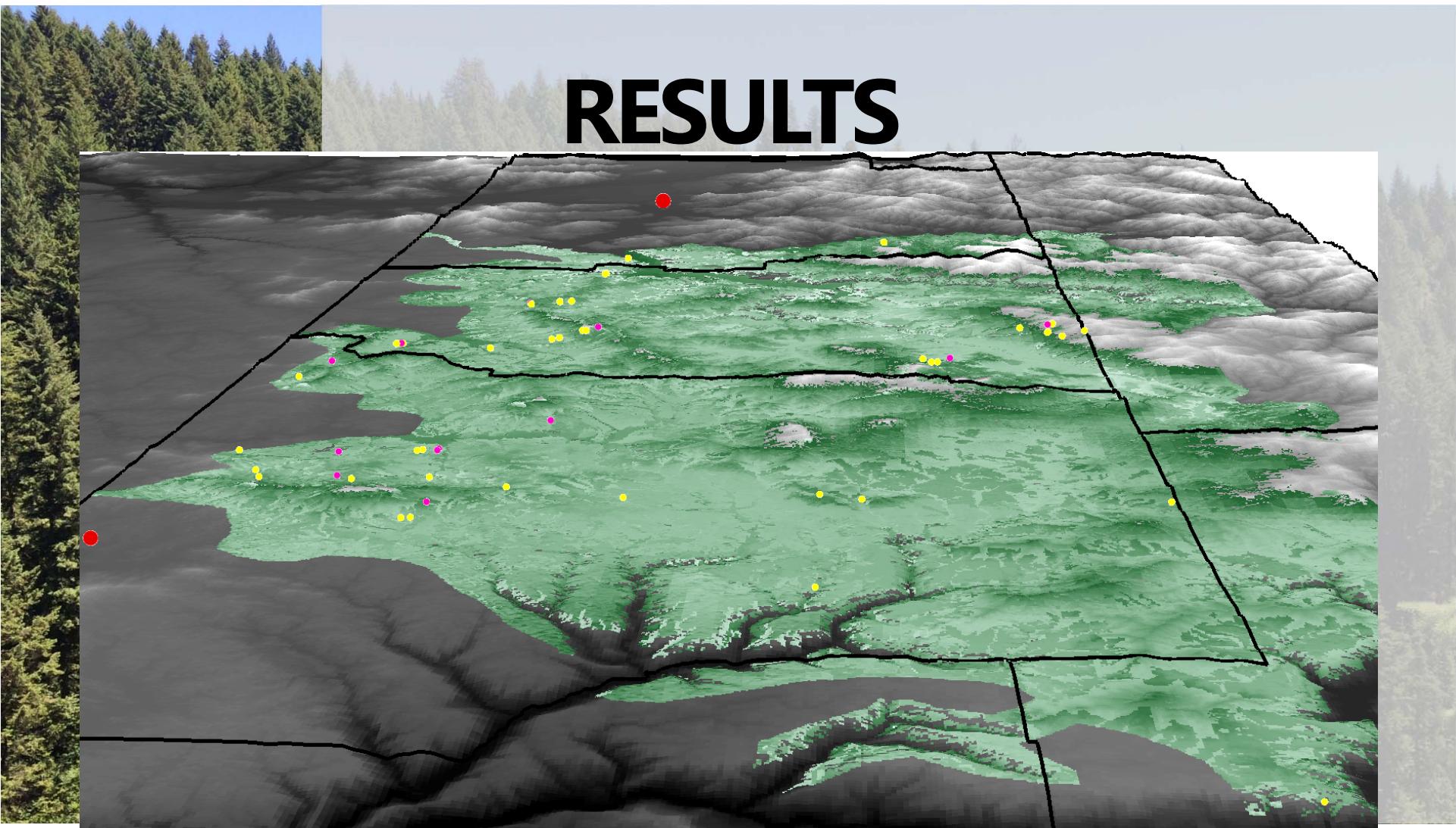
# RESULTS



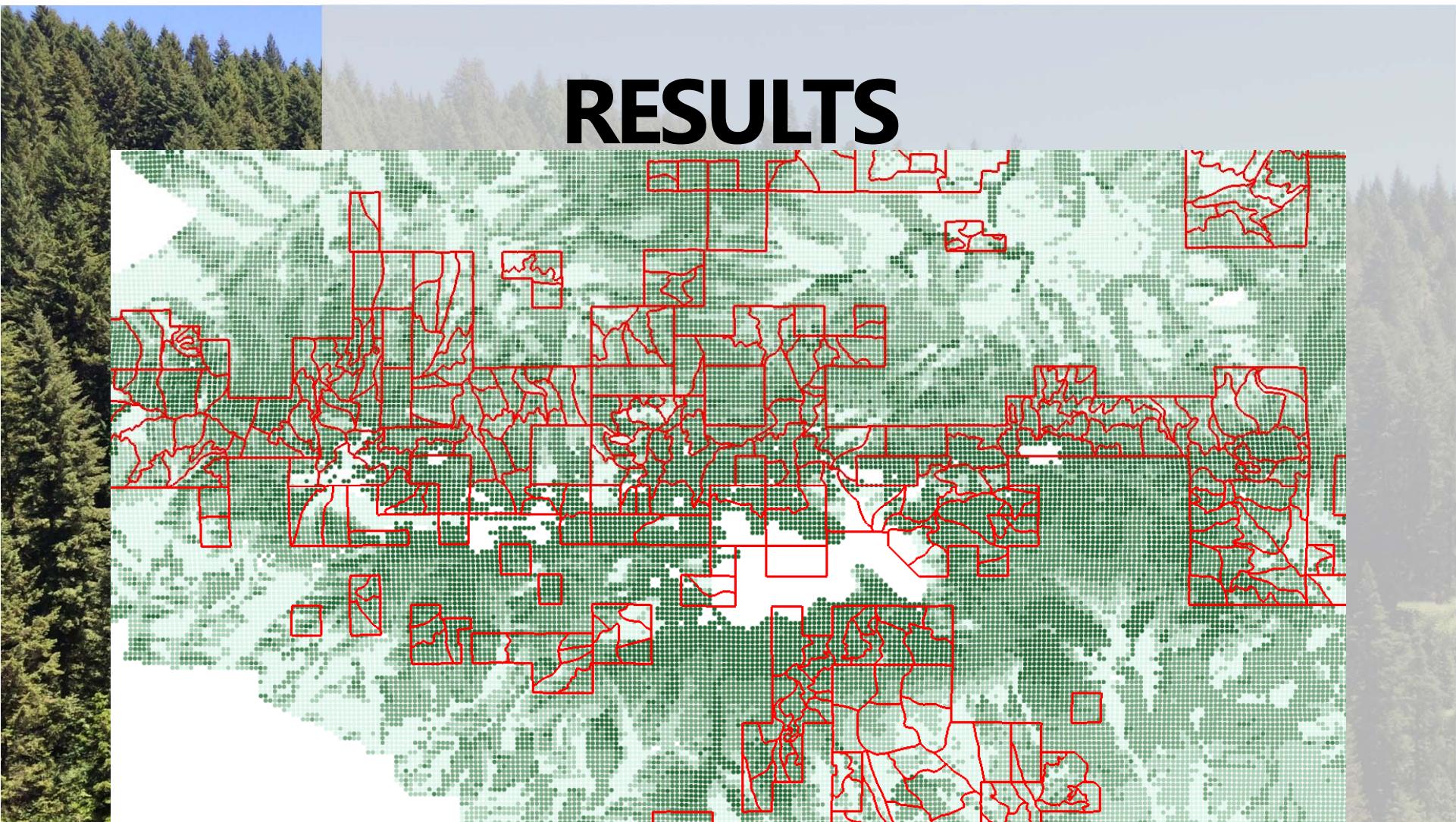


# RESULTS

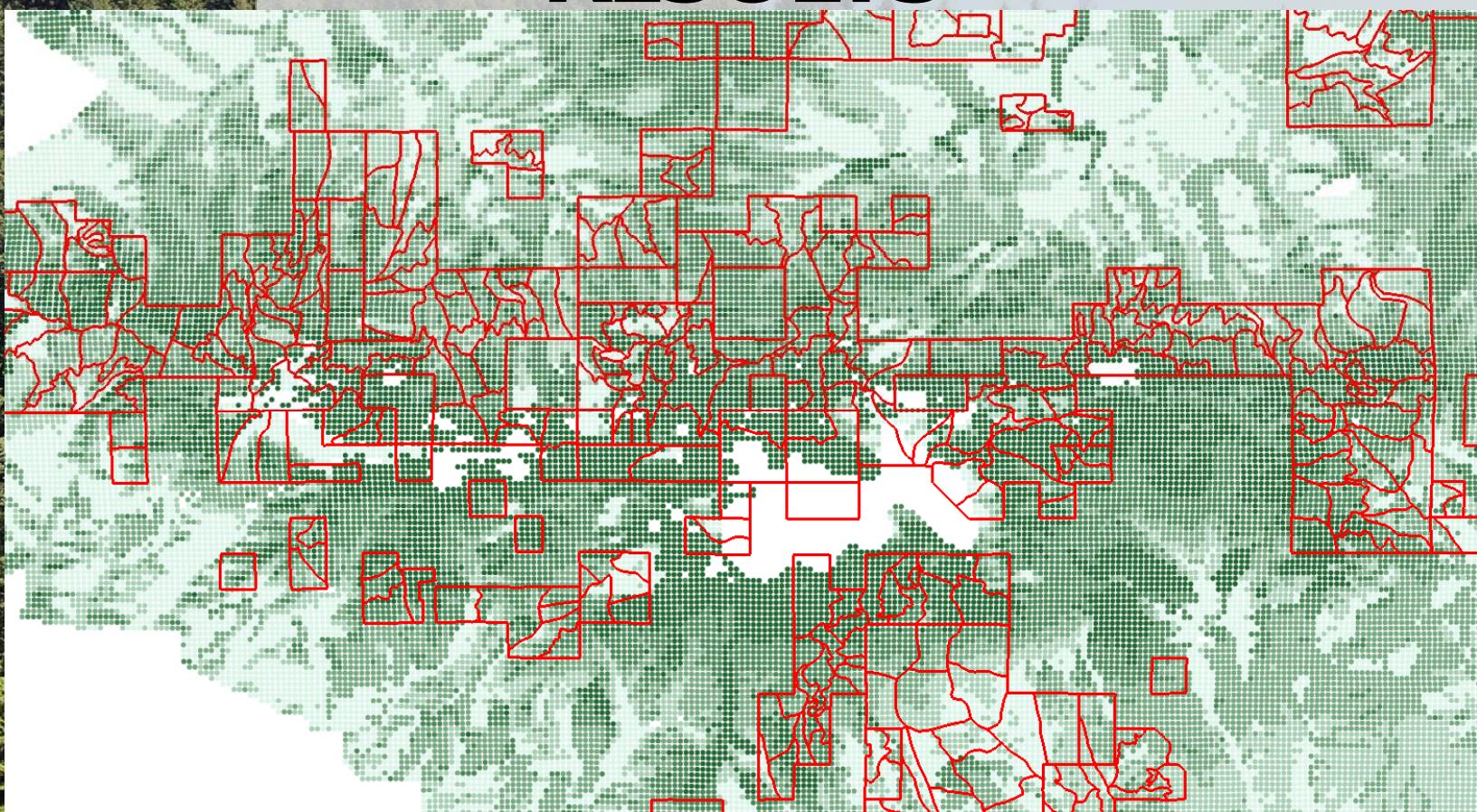




# RESULTS



# RESULTS





# SUMMARY



Available regional site index curves and equations are not accurately predicting tree height growth in our area.



A direct productivity measure: 10-meter site index



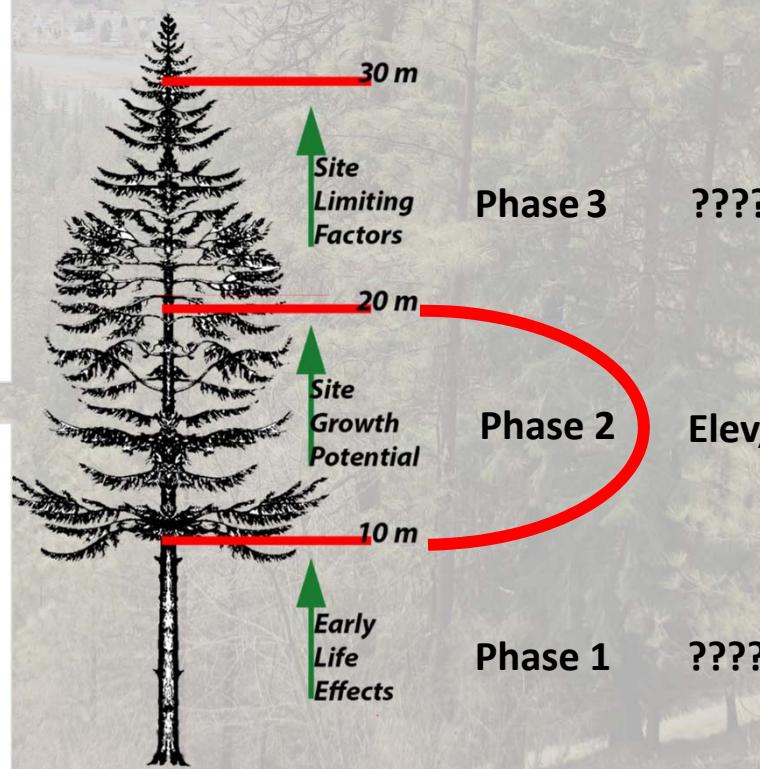
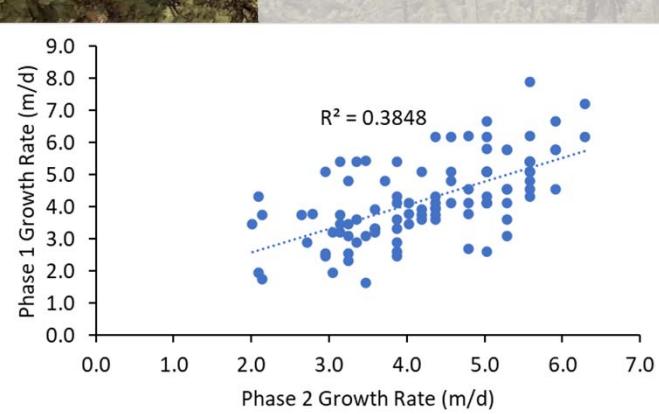
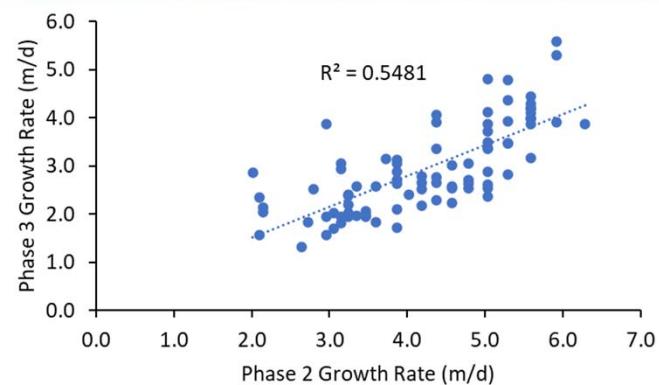
FPS prediction accuracy less than expected

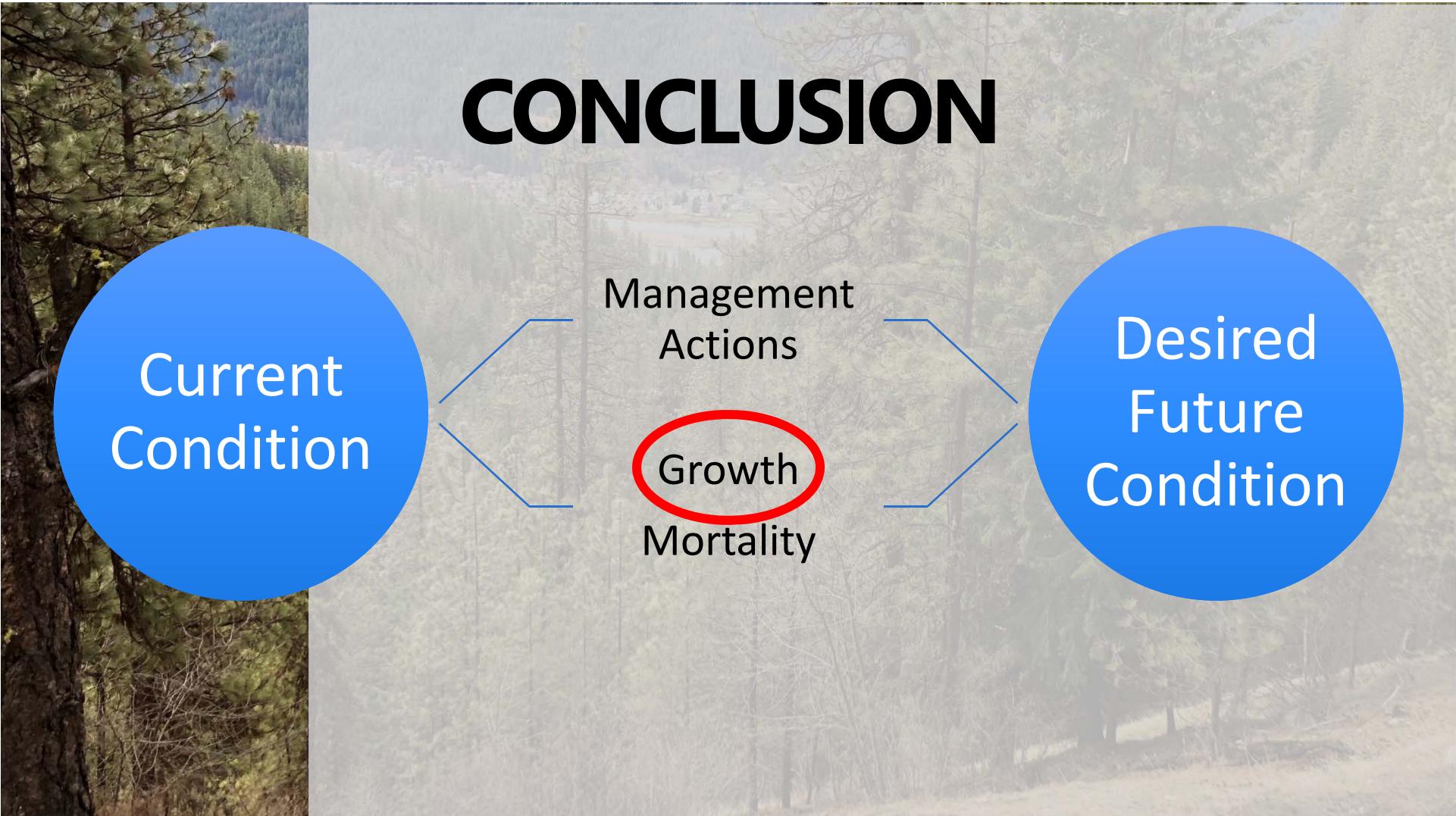
❖ Revisions to FPS are in the works to allow for smoothing span optimization



Fit and accuracy improved when elevation was added as a predictor and an optimum span value was chosen.

# FUTURE RESEARCH





# CONCLUSION

Current Condition

Management Actions

Growth

Mortality

Desired Future Condition



## ACKNOWLEDGEMENTS



**Bennett Lumber Products, Inc.**



**Forest Biometrics Research Institute**



**University of Idaho**



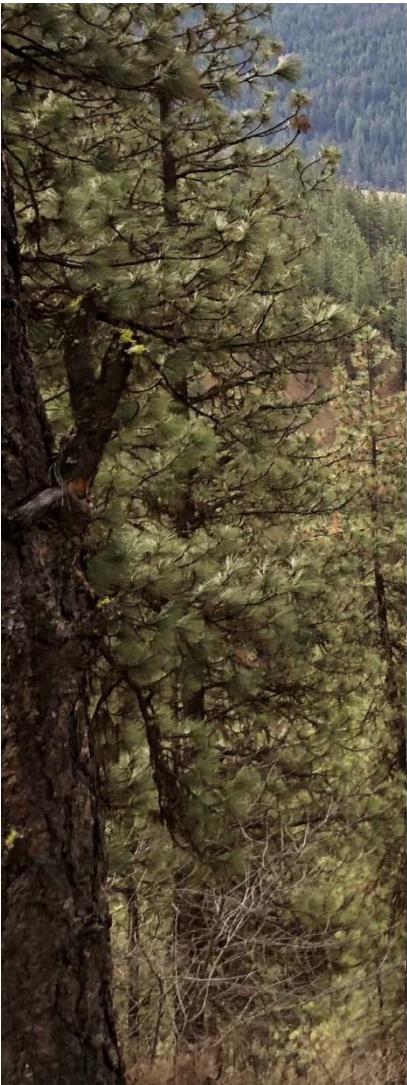
**Idaho Department of Lands**



**Ben Koester Logging**



**Mark Kimsey, Jim Arney,  
Ann Abbott, Andrew Nelson**



# QUESTIONS



# QUESTIONS



# REFERENCES

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